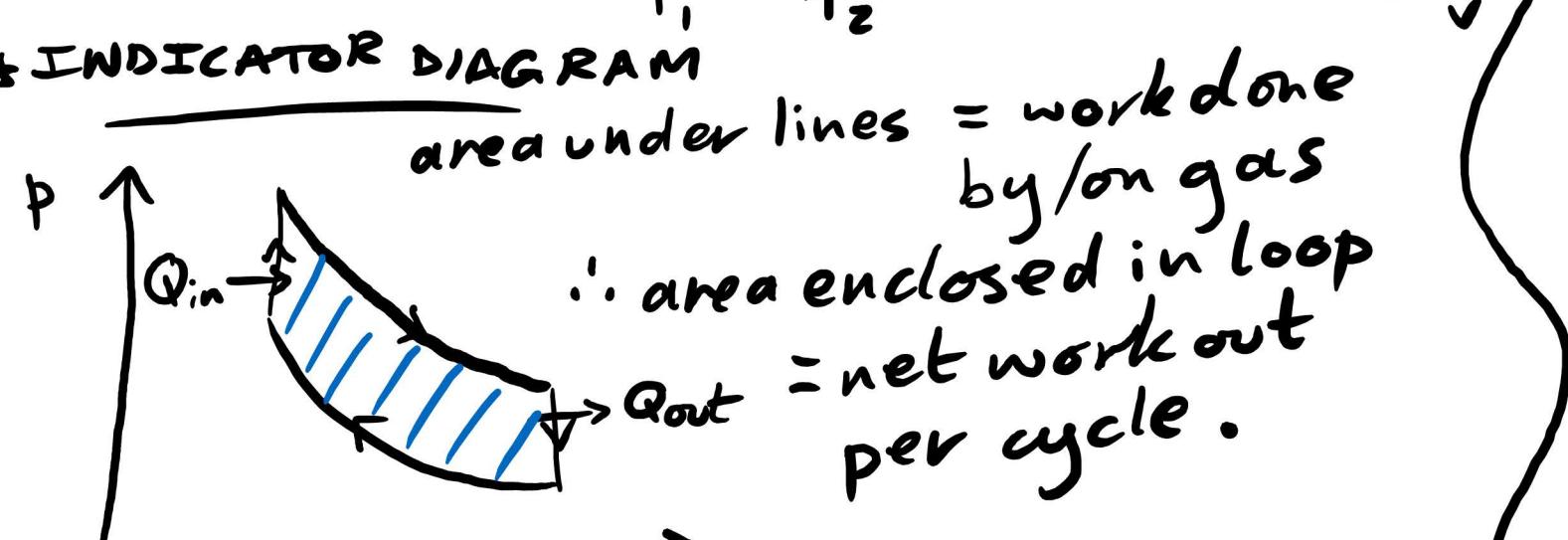


1st law of thermodynamics : $PV=nRT$

$$Q = U + W \leftarrow \begin{array}{l} \text{work done} \\ \text{by gas} \\ (-ve if compressed) \end{array}$$

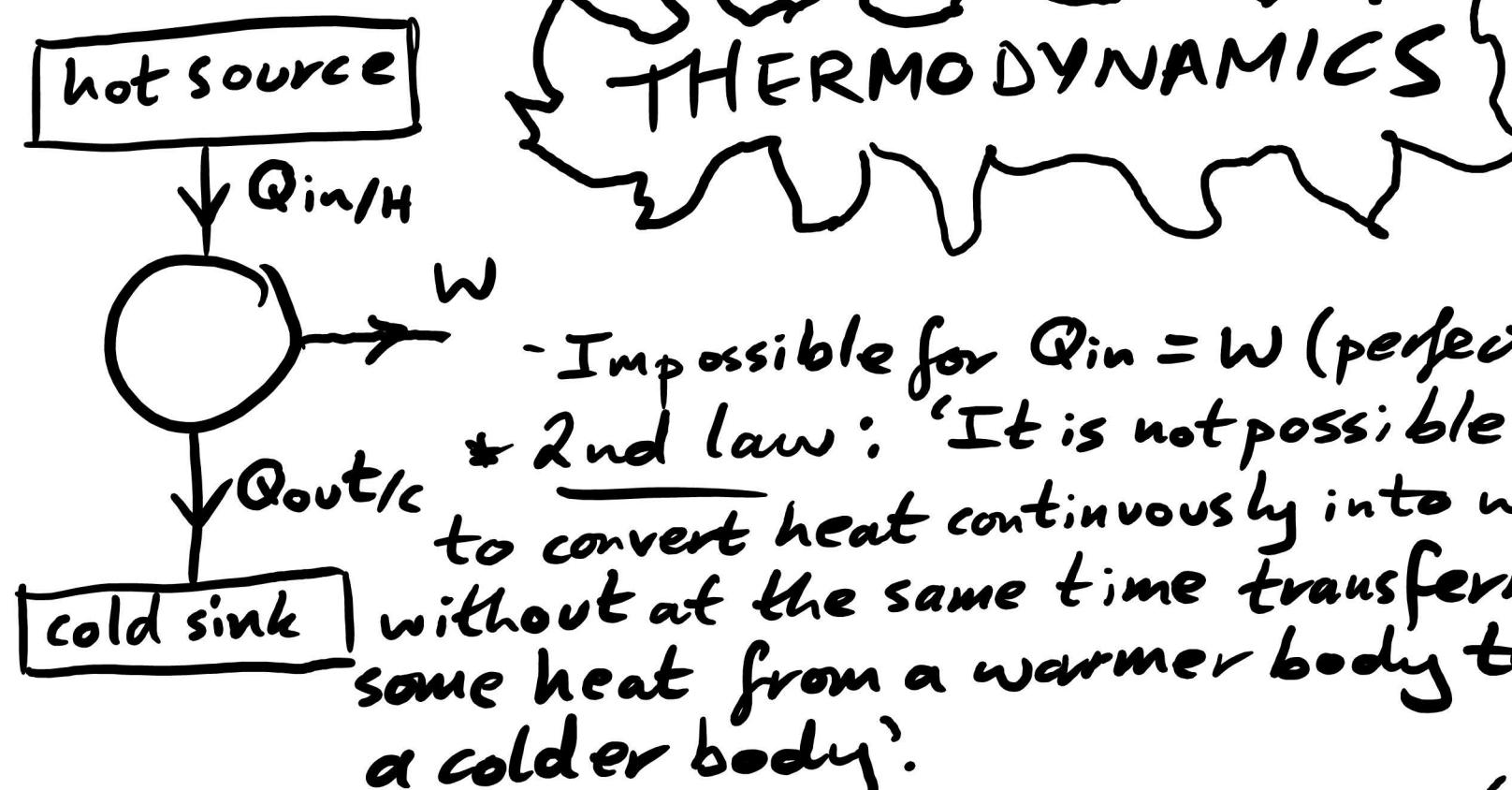
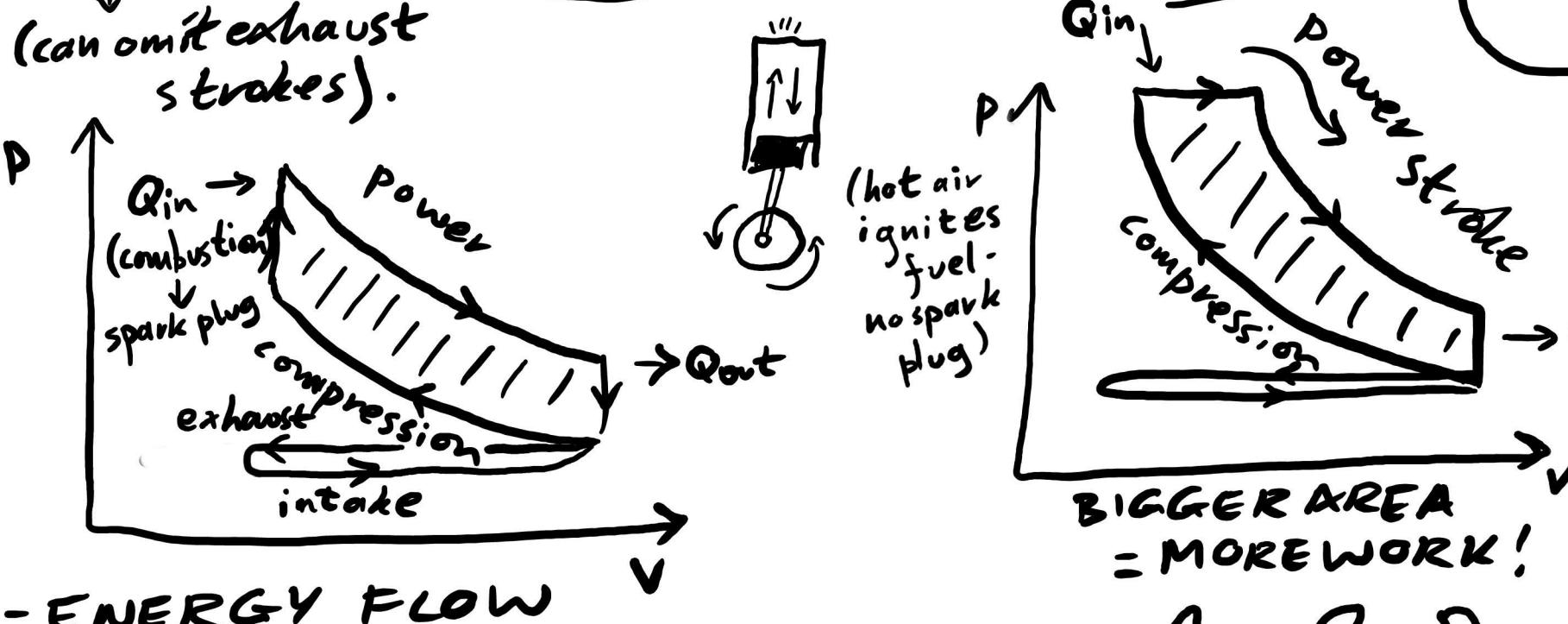
heat supplied $\rightarrow \Delta \text{internal E}$
 (-ve if heat removed)
 adiabatic constant
 - Adiabatic: $Q=0 \therefore -U=W \therefore p_1 V_1^\gamma = p_2 V_2^\gamma$
 - Isothermal: $U=0 \therefore Q=W \therefore p_1 V_1 = p_2 V_2$
 - Constant V: $W=0 \therefore Q=U \therefore \frac{p_1}{T_1} = \frac{p_2}{T_2} \uparrow T \uparrow$
 - Isobaric: $\Delta P=0 \therefore \frac{V_1}{T_1} = \frac{V_2}{T_2}$



Heat Engine: any device that causes net work to be done by gas by adding Q.

* OTTO CYCLE: PETROL ENGINES

(can omit exhaust strokes).



\therefore no engine can be 100% efficient.

* Max theoretical efficiency:

$$\epsilon = \frac{W}{Q_H} = \frac{Q_H - Q_C}{Q_H} = \frac{T_H - T_C}{T_H} \quad (\text{in } K!)$$

Coefficient of Performance
 efficiency equivalent
 COP = $\frac{Q_C}{W} = \frac{Q_H}{Q_H - Q_C} = \frac{T_H}{T_H - T_C}$
 heat pump \rightarrow better than electrical radiators

ROTATIONAL DYNAMICS

mass: 'how hard it is to get an object moving'
 moment of inertia: " " " " " " " " spinning'

Dimension	Linear equiv	Symbol	Unit	Equation
moment of inertia	mass	I	kgm^2	Ring/mass $I = mr^2$ Disc $I = \frac{1}{2}mr^2$
torque	Force	T	Nm	$T = I\alpha$ $T = Fr *$
angular disp.	disp.	θ	rad	
ang. vel.	velocity	ω	rad s^{-1}	$\omega = \frac{\Delta \theta}{t}$
ang. accn	accn	α	rad s^{-2}	$\alpha = \frac{\Delta \omega}{t}$
ang. momentum	momentum	L	$\text{kgm}^2 \text{s}^{-1}$	$L = I\omega$
work done	W or E	J	$\text{J} = T\theta$	
power	P	W	$P = Tw$	

suvat:

$$v = u + at$$

$$v^2 = u^2 + 2as$$

$$s = ut + \frac{1}{2}at^2$$

$$s = \frac{(u+v)t}{2}$$

$$\theta = \frac{\omega_1 + \omega_2}{2} t$$

$$w_2 = w_1 + \alpha t$$

$$w_2^2 = w_1^2 + 2\alpha \theta$$

$$s = v t + \frac{1}{2} \alpha t^2$$

$$\theta = \frac{\omega_1 + \omega_2}{2} t$$

$$* E_K = \frac{1}{2} I \omega^2 \Rightarrow \text{M}$$

$$\text{GPE} = E_K + E_K \text{ lost mass wheel} (+ \text{ work done wheel})$$

$$Mgh = \frac{1}{2} Mv^2 + \frac{1}{2} I\omega^2 (+ T\theta)$$

* Angular momentum coupling due to friction

Two spinning objects coupling, reach common ω . Total ang. momⁿ conserved, even if energy lost.

$$L_1 + L_2 = L_{12}$$

$$I_1 \omega_1 + I_2 \omega_2 = (I_1 + I_2) \omega_3$$

FLYWHEELS: needed to smooth torque resulting from linear \rightarrow rotational.
 - Stores E_K !



$$\text{COP}_{\text{fridge}} = \frac{Q_C}{W} = \frac{Q_C}{Q_H - Q_C} = \frac{T_H}{T_H - T_C}$$

* COMBINED HEAT & POWER
 Can use some work from engine to drive generator + heat pump: more efficient than just using electricity to heat.

